

4.14 Exercises and Problems

Q1/: For OP-AMP Signal Generation, fill the blank in the following in the table

No.	Resistances	V_{cc}	R_f	C	K	V_b	Frequency (F)
1.	$R_a = R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_1 =$	$V_{b1} =$	$F_1 =$
2.	$R_a = 2R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_2 =$	$V_{b2} =$	$F_2 =$
3.	$R_a = 3R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_3 =$	$V_{b3} =$	$F_3 =$

Ans:

$$K_1 = \frac{R_b}{R_a + R_b}, R_a = R_b, K_1 = \frac{R_a}{R_a + R_b} = \frac{1}{2}, V_{b1} = \pm K V_{cc} = \pm \frac{1}{2} \times 18 = \pm 9V$$

$$K_2 = \frac{R_b}{R_a + R_b}, R_a = 2R_b, K_1 = \frac{R_b}{2R_b + R_b} = \frac{1}{3}, V_{b2} = \pm K V_{cc} = \pm \frac{1}{3} \times 18 = \pm 6V$$

$$K_3 = \frac{R_b}{R_a + R_b}, R_a = 3R_b, K_1 = \frac{R_b}{3R_b + R_b} = \frac{1}{4}, V_{b3} = \pm K V_{cc} = \pm \frac{1}{4} \times 18 = \pm \frac{9}{2}V$$

$$F_1 = \frac{1}{T_1}, T_1 = 2R_f C \ln \frac{1+k_1}{1-k_1}, T_1 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/2}{1-1/2}, \\ F_1 = 455.1 \text{Hz}$$

$$F_2 = \frac{1}{T_2}, T_2 = 2R_f C \ln \frac{1+k_2}{1-k_2}, T_2 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/3}{1-1/3}, \\ F_2 = 721.3 \text{Hz}$$

$$F_3 = \frac{1}{T_3}, T_3 = 2R_f C \ln \frac{1+k_3}{1-k_3}, T_3 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/4}{1-1/4}, \\ F_3 = 978.8 \text{Hz}$$

Q2/: Design Summing op-amp circuit to solve the following equations

$$1. \quad V_o = 4V1 - 2V2 + 0.5V3 + V4$$

Consider the feedback resistance is equal to $10K\Omega$

Ans

$$V_o = 4V1 - 2V2 + 0.5V3 + V4$$

$$V_o = -\frac{R_f}{R1}V1 - \frac{R_f}{R2}V2 - \frac{R_f}{R3}V3 - \frac{R_f}{R4}V4$$

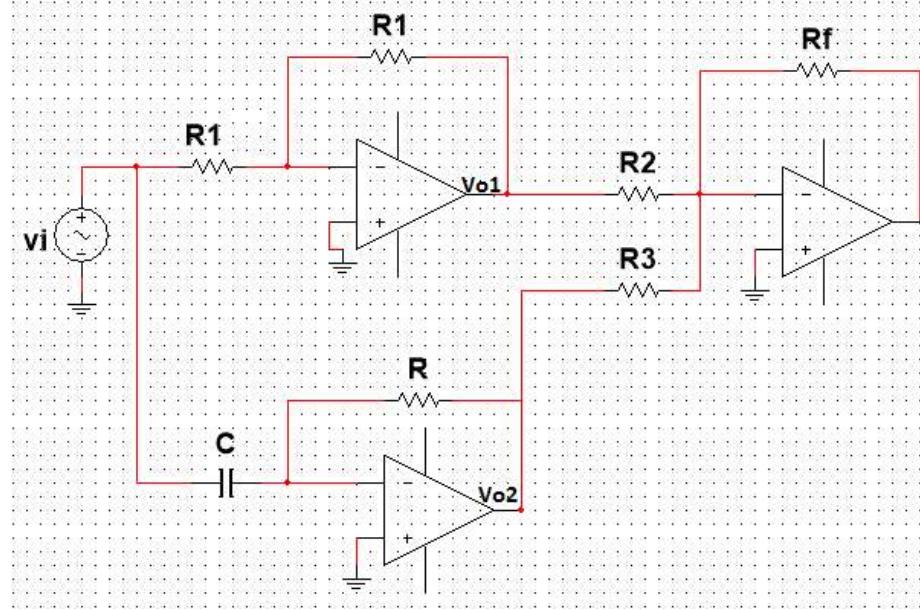
$$4 = \frac{R_f}{R1} \rightarrow 4 = \frac{10}{R1} \rightarrow R1 = 2.5K\Omega$$

$$2 = \frac{R_f}{R2} \rightarrow 2 = \frac{10}{R2} \rightarrow R2 = 5K\Omega$$

$$0.5 = \frac{R_f}{R3} \rightarrow 0.5 = \frac{10}{R3} \rightarrow R3 = 20K\Omega$$

$$1 = \frac{R_f}{R4} \rightarrow 1 = \frac{10}{R4} \rightarrow R4 = 10K\Omega$$

Q3/: Design Simple electronic circuit that given output Signal $v_o(t) = 5 \sin wt + 3 \cos wt$ from input signal $v_i(t) = \sin wt$ where $w = 10^4 \text{rad/sec}$.



$$v_{o2} = -RC \frac{d}{dx}(v_i(t)), \quad v_{o2} = -RCw \cos wt = -\cos wt$$

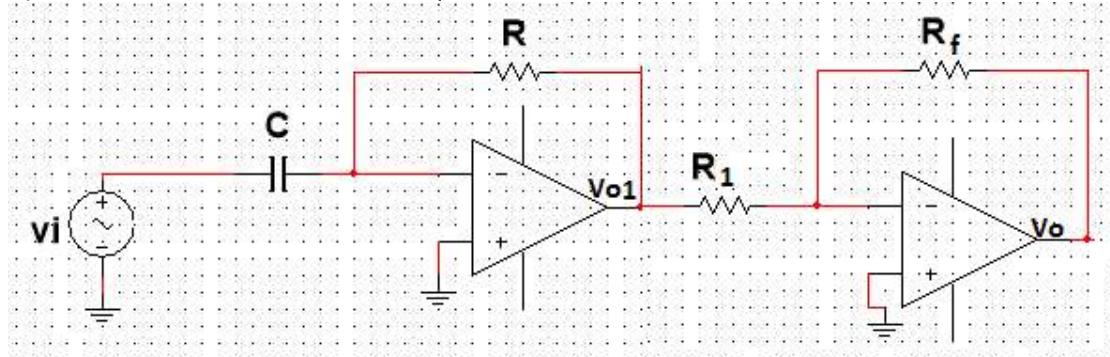
$$RCw = 1 \text{ let } C=5\text{nF}$$

$$R = \frac{1}{wc} \rightarrow R = 20K\Omega, \text{ let } R1 = 20K\Omega$$

$$\frac{R_f}{R2} = 5 \text{ let } Rf = 20K\Omega, R2 = 4K\Omega$$

$$\frac{R_f}{R2} = 3 \text{ let } Rf = 20K\Omega, R2 = 6.67K\Omega$$

Q4/: Design Simple electronic circuit that given output Signal $v_o(t) = 5 \cos wt$ from input signal $v_i(t) = \sin wt$ where $w = 10^4 \text{rad/sec}$.



$$v_{o1} = -RC \frac{d}{dx}(v_i(t)), \quad v_{o1} = -RCw \cos wt = -\cos wt$$

$$RCw = 1 \text{ let } C=5\text{nF}$$

$$R = \frac{1}{wC} \rightarrow R = 20K\Omega,$$

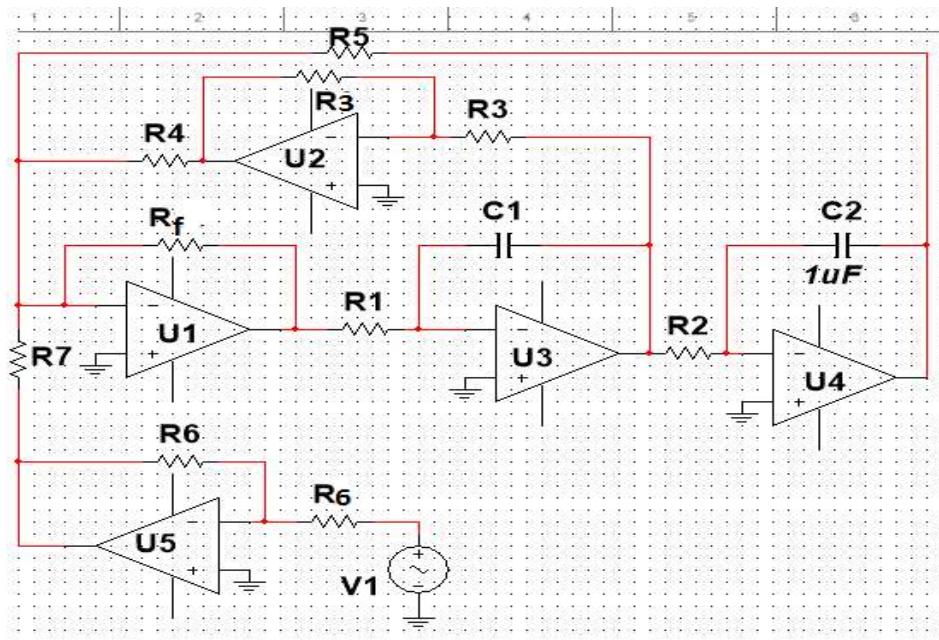
$$5 = \frac{R_f}{R_1} \text{ let } R_f = 20K\Omega \rightarrow R_1 = 4K\Omega$$

Q5/: Design electronic circuit to solve the following Differential equation

$$\frac{d^2y}{dt^2} + 4 \frac{dy}{dx} + 5y = 2\sin wt \text{ where , } y(0) = 1 \text{ volt and } \frac{dy}{dx}(0) = 0.5 \text{ volt}$$

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$$\frac{d^2y}{dt^2} = -4 \frac{dy}{dx} - 5y + 2\sin wt$$



$$\frac{1}{R_1 C_1} = 1 \rightarrow \text{let } C_1 = 10\mu F \rightarrow R_1 = 100K\Omega$$

$$\frac{1}{R_2 C_2} = 1 \rightarrow \text{let } C_2 = 10\mu F \rightarrow R_2 = 100K\Omega$$

Let $R_3 = 100K\Omega$, Let $R_6 = 100K\Omega$

$$\frac{R_f}{R_4} = 4 \rightarrow \text{let } R_5 = 20K\Omega$$

$$\frac{R_f}{R_7} = 2 \rightarrow \text{let } R_7 = 50K\Omega$$