

EX: The circuit shown in Figure below: - show that the output E_o is given as

$$E_o = \frac{2}{RC} \int E_i dt$$

Sol: -

$$V_1 = V_2 \quad (1)$$

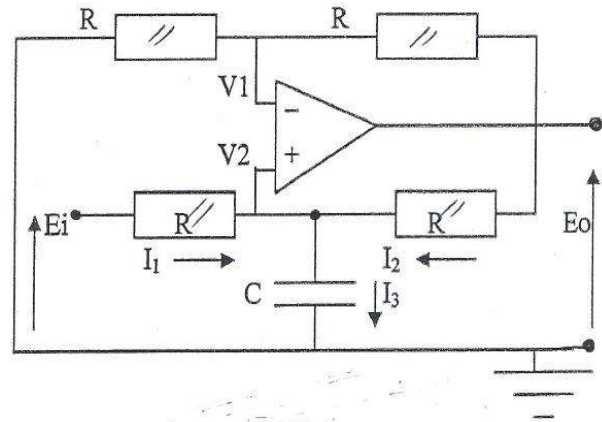
$$V_1 = \left[\frac{R}{R+R} \right] E_o = \frac{1}{2} E_o \quad (2)$$

$$I_1 + I_2 = I_3 \quad (3)$$

$$\frac{E_i - V_1}{R} + \frac{E_o - V_1}{R} = C \frac{dV_1}{dt} \quad (4)$$

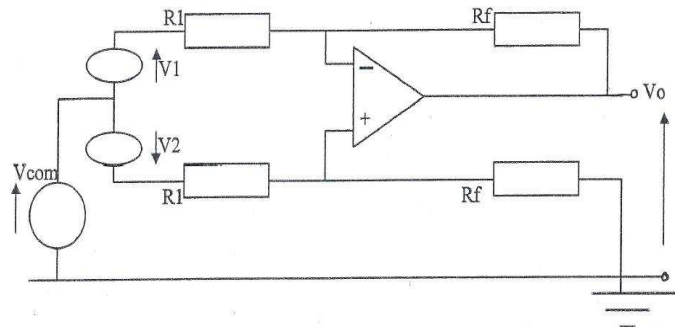
$$\frac{E_i - (\frac{1}{2})E_o}{R} + \frac{E_o - (\frac{1}{2})E_o}{R} = C \frac{d(\frac{1}{2})E_o}{dt}$$

$$E_o = \frac{2}{RC} \int E_i dt$$



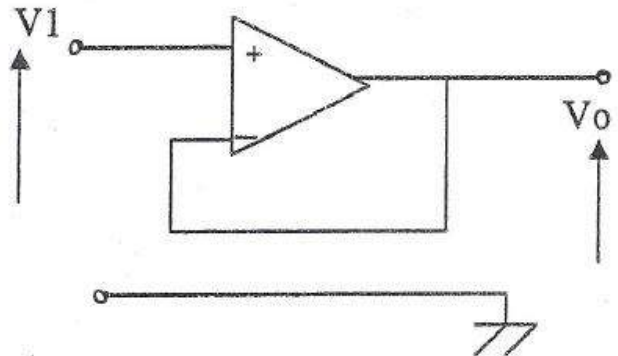
4.9 The differential OP-amp

$$V_o = [V_2 - V_1] \frac{R_f}{R_1}$$



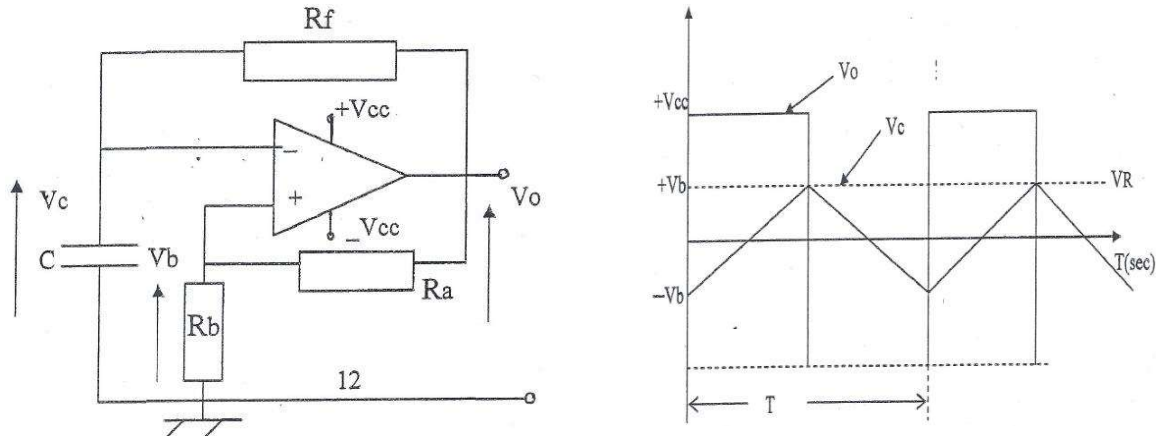
4.10 Op-amp voltage follower

$$V_o = V_1$$



4.11 Op-amp Signal Generator

OP-AMP Signal Generator:- It has negative and positive feedback circuits (a) R_f = negative feedback resistance and (b) K = positive feedback coefficient, $K = \frac{R_b}{R_a + R_b}$ see figure bellow.



V_b = non-linear input of the op-amp (v)

$$V_b = kV_o = \pm kV_{cc} \quad (1)$$

T = the periodic time of the output/input signals (sec)

$$T = 2R_f C \ln \frac{1+k}{1-k} \quad (2)$$

F = Frequency of the generated signals (Hz)

$$F = \frac{1}{T} \quad (3)$$

EX :- Op-amp signal generator, if $R_a=R_b$, $R_f = 10K\Omega$, $C = 0.1\mu F$, and $V_{cc} = \pm 18V$; Find (1) V_b and (2) Frequency F

Sol.

$$(1) V_b = kV_o = \pm kV_{cc}$$

$$K = \frac{R_b}{R_a + R_b} = 0.5$$

$$V_b = \pm 0.5 \times 18 = \pm 9$$

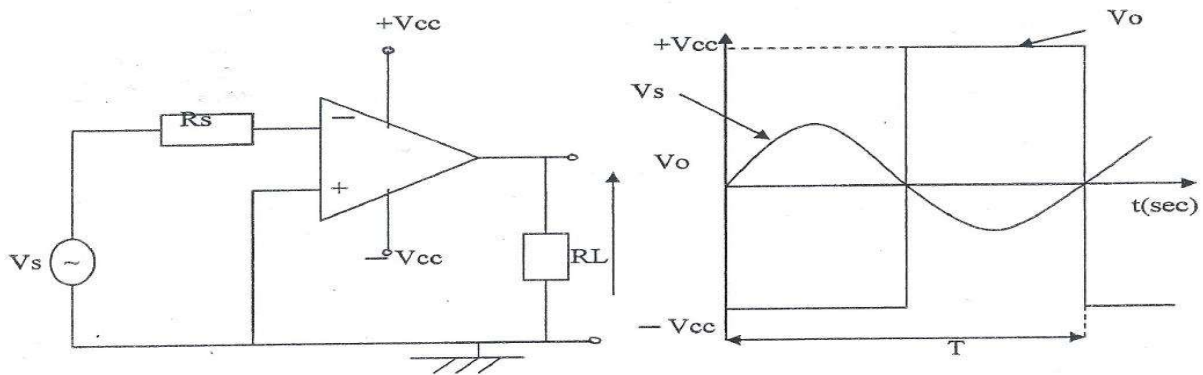
$$(2) T = 2R_f C \ln \frac{1+k}{1-k}$$

$$T = 2 \times 10 \times 10^4 \times 0.1 \times 10^{-6} \ln \frac{1+0.5}{1-0.5} = 2.197 \times 10^{-3}$$

$$F = \frac{1}{T} = \frac{1}{2.197 \times 10^{-3}} = 455 \text{ Hz}$$

4.12 Op-amp Zero Crossing Detector

OP-AMP Zero Crossing Detector: -This is one of the open loop applications of op-amp, also called sinewave to square wave converter.



$$V_o = \pm V_{cc} \text{ and } F_o = F_i = 1/T = \omega/2\pi$$

EX:- Op-amp, Zero crossing detector has $V_{cc} = \pm 15v$, $V_s = 5\sin 377t$ (a) Draw the power circuit diagram, (b) Sketch the input-output waveforms (c) Calculate F_o

Sol: -

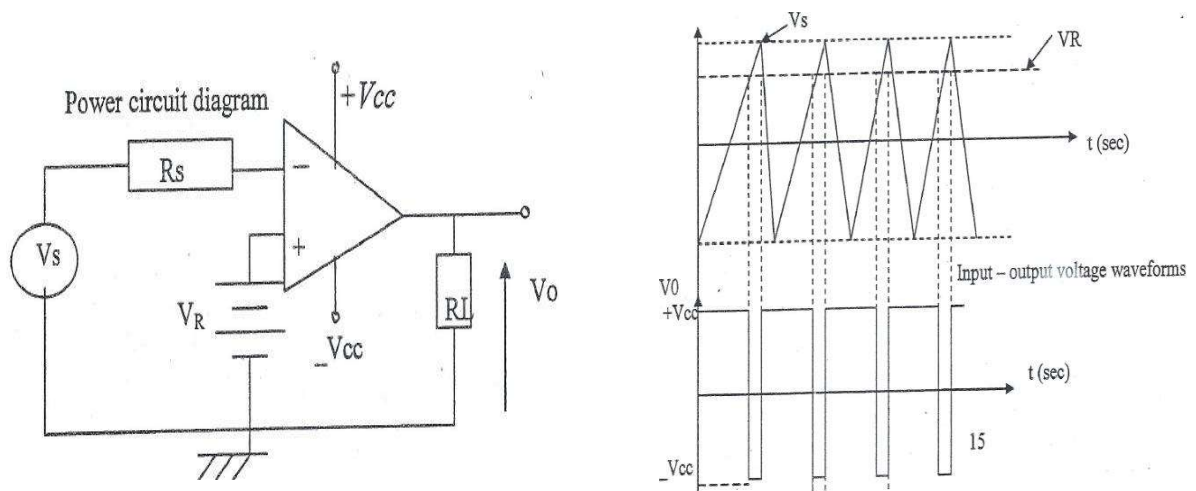
(a) And (b) as shown in Figure above (previous slide)

(c) $F_o = F_i = 1/T = \omega/2\pi$, $\omega = 377$

$$F_o = 377 / (2 \times 3.14) = 60\text{Hz}$$

4.13 The Comparator

The Comparator: - This is also one of the open loop applications of op-amp, it is used to compare two voltages one of it's a dc voltage called reference voltage [V_R]



4.14 Exercises and Problems

Q1/: For OP-AMP Signal Generation, fill the blank in the following in the table

No.	Resistances	V_{CC}	R_f	C	K	V_b	Frequency (F)
1.	$R_a = R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_1 =$	$V_{b1} =$	$F_1 =$
2.	$R_a = 2R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_2 =$	$V_{b2} =$	$F_2 =$
3.	$R_a = 3R_b$	± 18	$10K\Omega$	$0.1\mu F$	$K_3 =$	$V_{b3} =$	$F_3 =$

Ans:

$$K_1 = \frac{R_b}{R_a + R_b}, \quad R_a = R_b, \quad K_1 = \frac{R_a}{R_a + R_a} = \frac{1}{2}, \quad V_{b1} = \pm K V_{CC} = \pm \frac{1}{2} \times 18 = \pm 9v$$

$$K_2 = \frac{R_b}{R_a + R_b}, \quad R_a = 2R_b, \quad K_2 = \frac{R_b}{2R_b + R_b} = \frac{1}{3}, \quad V_{b2} = \pm K V_{CC} = \pm \frac{1}{3} \times 18 = \pm 6v$$

$$K_3 = \frac{R_b}{R_a + R_b}, \quad R_a = 3R_b, \quad K_3 = \frac{R_b}{3R_b + R_b} = \frac{1}{4}, \quad V_{b3} = \pm K V_{CC} = \pm \frac{1}{4} \times 18 = \pm \frac{9}{2}v$$

$$F_1 = \frac{1}{T_1}, \quad T_1 = 2R_f C \ln \frac{1+k_1}{1-k_1}, \quad T_1 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/2}{1-1/2},$$

$$F_1 = 455.1\text{Hz}$$

$$F_2 = \frac{1}{T_2}, \quad T_2 = 2R_f C \ln \frac{1+k_2}{1-k_2}, \quad T_2 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/3}{1-1/3},$$

$$F_2 = 721.3\text{Hz}$$

$$F_3 = \frac{1}{T_3}, \quad T_3 = 2R_f C \ln \frac{1+k_3}{1-k_3}, \quad T_3 = 2 \times 10 \times 10^3 \times 0.1 \times 10^{-6} \ln \frac{1+1/4}{1-1/4},$$

$$F_3 = 978.8\text{Hz}$$

Q2/: Design Summing op-amp circuit to solve the following equations

1. $V_o = 4V_1 - 2V_2 + 0.5V_3 + V_4$

Consider the feedback resistance is equal to $10K\Omega$

Ans

$$V_o = 4V_1 - 2V_2 + 0.5V_3 + V_4$$

$$V_o = -\frac{R_f}{R_1}V_1 - \frac{R_f}{R_2}V_2 - \frac{R_f}{R_3}V_3 - \frac{R_f}{R_4}V_4$$

$$4 = \frac{R_f}{R_1} \rightarrow 4 = \frac{10}{R_1} \rightarrow R_1 = 2.5K\Omega$$

$$2 = \frac{R_f}{R_2} \rightarrow 2 = \frac{10}{R_2} \rightarrow R_2 = 5K\Omega$$

$$0.5 = \frac{R_f}{R_3} \rightarrow 0.5 = \frac{10}{R_3} \rightarrow R_3 = 20K\Omega$$

$$1 = \frac{R_f}{R_4} \rightarrow 1 = \frac{10}{R_4} \rightarrow R_4 = 10K\Omega$$